

Felix Hausdorff 1868-1942 (died 26.01.1942)

- 1910 Leipzig ; 1910-1913 Bonn ; 1913-1921 Greifswald  
1921- Bonn

~ 42 publications (of which ~12 in analysis)  
in maths.

+ Grundzüge 1914 + Mengenlehre 1927, 1935 + several (4) vols. essay  
poetry, drama etc. 1897-1910 under the name Paul Mongré

~ 26'000 pages Nachlass (Findbuch)

1 + 8 vols. collected works: I. General, set theory  
Brieskorn, Hirzebruch, Remmert, Parker, Scholz  
✓ IV Analysis, alg., no. th. V. Astronom. Optics, prob. 2004?  
✓ VI Geometry etc. Reum Zeit VII + VIII Literary  
IX Korrespondenz Phil. Werk 2004  
Baker-Campbell-H. formula 1906

H. spaces, H. paradox } 1914 Grundzüge  
H. max. principle, H. distance }

H. measures, dimension 1919

Toeplitz-Hausdorff thm. 1919

H. summability 1921, H. moment problem 1923

H.-Young inequality 1923.

First 4 papers on astronomy & optics 1891-96, doct. with H. Bruns (1848-1919)  
Begins with set theory ~ 1907.

$$I = \int_{-\infty}^{\infty} \frac{\sin(x-\beta) \cdot \sin(x-\gamma)}{(x-\beta)(x-\gamma)} dx = \pi \frac{\sin(\gamma-\beta)}{(\gamma-\beta)}$$

Borel 1871-1956

Baire 1874-1932

Lebesgue 1875-1941

Banach 1892-1945

Tarski 1901-1983

Klein 1849-1925

Hilbert 1862-1943

Cantor 1845-1918

Fréchet 1878-1973

F. Riesz 1880-1956

Weyl 1885-1955

Lindelberg (1876-1932)

"Aus dem Paradies, das Cantor uns  
geschaffen, soll uns niemand vertreiben können."  
Hilbert 1925

"Je me détourne avec effroi et horreur  
de cette place lamentable des fonctions qui  
n'ont pas de dérivées" Hermite à Stieltjes.

"prinzipiell ganz unklar" Hausdorff  
1923

Bismarck (1815-1898, 1871)

Wilhelm II (1859-1941)

Hitler (1889-1945)

Band VII (2004) Philosophisches Werk Paul Mongré (Pseudonym)

1897 Sant'Ilario Gedanken aus der Landschaft Zarathustras  
~ 379 S.

1898 Das Chaos in kosmischer Auslese - Ein erkenntnistheoretischer Versuch.  
Essays zu Nietzsche (Ed. Werner Stegmayer)  
Phil. Inst. Greifswald

Deutsche Forschungsgemeinschaft  
Akademie der Wissenschaften  
Nordrhein-Westfalen

Band VIII Literarisches Werk

1900 Ekstasen (Gedichtband)  
~ 216 S.

1904 Theaterstücke  
Bellettristik

BCH formula  $e^x e^y = e^z$   
$$z = x + y + \frac{1}{2}[x, y] + \frac{1}{12}[[x, y], y] + \frac{1}{12}[[y, x], x] + \dots$$

T-H thm.  
$$W(\mathcal{I}) = \{ \langle Tz, z \rangle : z \in \mathbb{C}^m, \|z\| = 1 \}$$
 convex, comp. in  $\mathbb{C}$   
$$\langle a, b \rangle = \sum_{j=1}^m a_j \bar{b}_j$$
  
$$\|a\| = \sqrt{\langle a, a \rangle}$$

H.-Y. inequality

$$\|\hat{F}\|_{p'} \leq \|F\|_p$$

$$1 \leq p \leq 2$$

(Chatterji, *Ens. Math.*  
46 (2000))

SJC Math. Semesterberichte 2002 (Vol 49)

Scholz EMS Newsletter (March 2005)

1914  $S = A \cup B \cup C \cup D$  (disjoint),  $D$  den.,  $A \sim B \sim C \sim (B \cup C)$

Banach 1923, Banach-Tarski 1924, Neumann 1929 amenable groups (other work on measure theory if time permits)

1919  $\lambda: [0, \infty[ \rightarrow [0, \infty[$ ,  $\lambda \uparrow$ ,  $\lambda(0+) = 0$

$$L^\lambda(A) = \lim_{\epsilon > 0} \inf \left\{ \sum_{n=1}^{\infty} \lambda(d_n) : d_n = \text{diam}(A_n), \bigcup_n A_n \supset A, A_n \text{ open ball} \right\}$$

$A$  has dim.  $[\lambda]$  if  $0 < L^\lambda(A) < \infty$ .

If  $\lambda$  conts, concave,  $\frac{\lambda(x)}{x} \rightarrow \infty$  ( $\lambda(x) = x^p$ ,  $0 < p < 1$ ) then  $\exists A \subset \mathbb{R}$ ,

dim  $A = [\lambda]$ . Dvoretzky 1948  $\liminf_{z \rightarrow 0+} \frac{\lambda(x)}{x^q} > 0 \Rightarrow \exists A \subset \mathbb{R}^q$   
( $= \infty$  case imp.)

Rogers 1998 general  $\lambda$

$$\lambda(x) = e^{-1/x}, \quad \frac{\lambda(x)}{x^q} \rightarrow 0 \quad \forall q.$$

Cantor set has dim  $\frac{\log 2}{\log 3} = 0.63\dots$

$$\alpha = \sup \{ p > 0 : L^{(p)}(A) = \infty \} = \inf \{ p > 0 : L^{(p)}(A) = 0 \}$$

1923 H. moment problem  $\int_0^1 x^n d\mu(x) = \mu_n$ ,  $n=0,1,\dots$

$$\Delta^n \mu_n \geq 0$$

$$\int_0^1 x^n d\mu(x) = \mu_n$$

$$t_0 = 0, t_n > 0, \sum \frac{1}{t_n} = \infty$$

Müntz (1884-1931) ~ 1914

$$\Delta^n = (I - E)^n = \sum_{k=0}^n (-1)^k \binom{n}{k} E^k$$

$$\begin{bmatrix} 1 & 0 & 0 & \dots \\ 1 & -1 & 0 & \dots \\ 1 & -2 & 1 & 0 \\ 1 & -3 & 3 & -1 & 0 \\ \dots & \dots & \dots & \dots & \dots \end{bmatrix}$$

1921 H. matrix

$$\lambda = \rho^{-1} \mu \rho$$

$$\rho = \rho^{-1} = \begin{bmatrix} \rho \\ \rho, m \end{bmatrix}$$

$$\rho_{p,m} = \begin{cases} \binom{p}{m} (-1)^m & 0 \leq m \leq p \\ 0 & m > p \end{cases}$$

$$\mu = \text{diag}(\mu_0, \mu_1, \dots)$$

$\lambda$  Conv pres  $\Leftrightarrow \mu$  moment-sep.  
reg.  $\Leftrightarrow$  " +  $\chi([0,1]) = 1, \chi(\{0\}) = 0$

Knopp-Schnoe thm. 1907 1904

$$C_\alpha : \mu_n = \frac{1}{\binom{n+\alpha}{n}}, \alpha > 0$$

$$H_\alpha : \mu_n = \frac{1}{(n+1)^\alpha}$$

$\alpha > 0$

$C_\alpha \sim H_\alpha$

1923

Toeplitz-H. thm.

$$W(C) = \{ \langle z, z \rangle : z \in \mathbb{C}^n, \|z\| = 1 \} \subset \mathbb{C}^{\text{complex}}$$